Study Guide 4

Optimization

1. Find the critical points and critical values of the following functions.

a. $f(x) = 3x^2 - 4x + 2$ **b.** $g(t) = 2t^3 - 9t^2 - 24t + 7$ **c.** $y = 5xe^{-0.125x^2}$ **d.** $w = \frac{9u}{4+5u} - u$

- 2. Use the *first derivative test* to classify the critical values that you found in 1c. and 1d. as relative minimum values, relative maximum values or neither.
- **3.** Use the *second derivative test* to classify the critical values that you found in 1a. and 1.b. as relative minimum values, relative maximum values or neither.
- 4. Find the absolute maximum and minimum values of function $f(x) = 2x^3 3x^2 12x + 11$ on the interval [0, 10]. Justify your claim.
- 5. Find the *absolute minimum* value of the function $c = 0.1q + 15 + \frac{100}{q}$ in the interval $(0, \infty)$. Justify your claim.
- **6.** Consider the function $v = u^2 e^{-5u}$
 - **a.** Does v have an absolute maximum value in the interval $(0, \infty)$? If so, find it and justify your claim. If not, explain why not.
 - **b.** Does v have an absolute *minimum* value in the interval $(0, \infty)$? If so, find it and justify your claim. If not, explain why not.
 - c. Does v have an absolute maximum value in the interval $(-\infty, \infty)$? If so, find it and justify your claim. If not, explain why not.
 - **d.** Does v have an absolute *minimum* value in the interval $(-\infty, \infty)$? If so, find it and justify your claim. If not, explain why not.